Progression in Calculation: Fractions, Decimals and Percentages

Vocabulary: The vocabulary listed for each year group is intended as a guide to what pupils should know but is not exhaustive. It is expected that key vocabulary is displayed on 'Maths Walls' at appropriate times during the year, and is promoted through mathematical talk in lessons and included in powerpoints

Primary Progression - Fractions, Decimals, Percentages



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions: Calculations		• write simple fractions for example, $\frac{1}{2}$ of $6 = 3$	• add and subtract fractions with the same denominator within one whole [for example, $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$]	add and subtract fractions with the same denominator	add and subtract fractions with the same denominator and denominators that are multiples of the same number multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	 add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions multiply simple pairs of proper fractions, writing the answer in its simplest form [for example \frac{1}{24} \times \frac{1}{2} = \frac{1}{8}] divide proper fractions by whole numbers [for example, \frac{1}{3} \div 2 = \frac{1}{6}]
		Spring 4	Summer 1	Spring 3	Spring 3	Autumn 3

Primary Progression – Fractions, Decimals, Percentages



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Decimals: Calculations & Problems				find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths	solve problems involving number up to three decimal places	multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places multiply one-digit numbers with up to two decimal places by whole numbers use written division methods in cases where the answer has up to two decimal places solve problems which require answers to be rounded to specified degrees of accuracy
				Spring 4	Summer 1	Spring 1

Primary Progression – Fractions, Decimals, Percentages



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions, Decimals and Percentages				solve simple measure and money problems involving fractions and decimals to two decimal places	 recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal solve problems which require knowing percentage and decimal equivalents of \$\frac{1}{2}, \frac{1}{4}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5}\$ and those fractions with a denominator of a multiple of 10 or 25 	associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, \frac{3}{8}] recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
Fracti				Spring 3 Spring 4 Summer 1	Spring 3	Spring 1 Spring 2

Primary Progression – Fractions, Decimals, Percentages



	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fractions, Decimals and Percentages				solve simple measure and money problems involving fractions and decimals to two decimal places	 recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal solve problems which require knowing percentage and decimal equivalents of \$\frac{1}{2}, \frac{1}{4}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5}\$ and those fractions with a denominator of a multiple of 10 or 25 	associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, $\frac{3}{8}$] recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
Fracti				Spring 3 Spring 4 Summer 1	Spring 3	Spring 1 Spring 2

Year 2: National Curriculum: Fractions Recognise, find, name and write fractions 1/3, 1/4, 2/4 and 3/4 of a length, shape, set of objects or quantity write simple fractions for example, 1/2 of 6 = 3 and recognise the equivalence of 2/4 and 1/2.

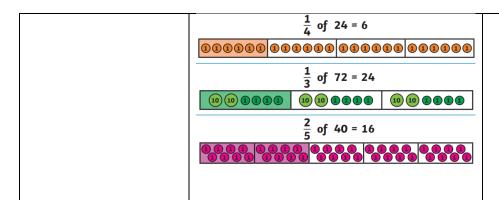
Key vocabulary: Whole, equal parts, one half, two halves, one third, two thirds, a quarter, two quarters, three quarters, equivalence, equivalent

Objective and Strategies	Concrete	Pictorial	Abstract
Year 2 Write simple fractions of amounts	Using cubes to calculate \(\frac{1}{4} \) of 36:	Drawing dots to find $\frac{1}{3}$ of 18: 18 18 18 18 6 6 6 6 Write the number of dots you have in each part. Then, circle the number of parts you need.	½ of 90 = 45
	Using cubes to calculate $\frac{2}{4}$ of 36: 36 9 9 9	Drawing dots to calculate $\frac{3}{4}$ of 24: 24 6 6 6 6 $\frac{1}{4}$ of 8 $\frac{1}{4}$ of 20 $\frac{1}{4}$ of 40 8 20 40 2 2 2 2 2 5 5 5 5 10 10 10 10 10	

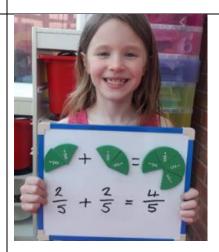
Year 3: National Curriculum: Fractions count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 * recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators are recognise and show, using diagrams, equivalent fractions with small denominators and and subtract fractions with the same denominator within one whole [for example, 5/7 + 1/7 = 6/7] * compare and order unit fractions, and fractions with the same denominators solve problems that involve all of the above.

Key vocabulary: numerator, denominator, unit fraction, non-unit fraction, compare and order, halves, thirds, quarters, fifths, sixths, eighths, tenths

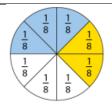
Objective and Strategies	Concrete	inparo ana		orial	, quartoro,	111110,	Abstract
Y3 Fractions of amounts	3 of 30 = 18 Use a bar model and place value counters to find e.g. one quarter of 84 (tens and ones counters)	21	21	21	21		1/4 of 84 = 21

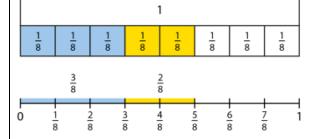


Y3 Adding fractions with the same denominator within one whole



Using fraction circles





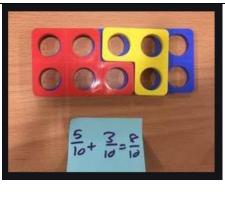
Numerator (1 for a unit fraction)

- 1 ← One of the parts of the whole
- **2** ← Denominator

The number of equal parts in the whole

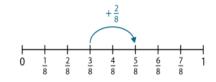
Adding fractions:

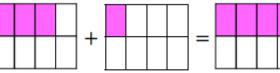
- ' $\frac{6}{10}$ is six lots of $\frac{1}{10}$.'



Using numicon

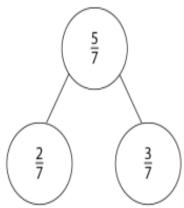
Number line:





We can use this model to calculate $\frac{3}{8} + \frac{1}{8} = \frac{4}{8}$

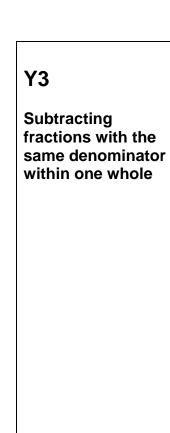
Part-part-whole model:



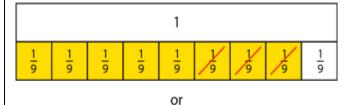
$$\frac{1}{8} + \frac{1}{8} + \frac{3}{8} = \boxed{}$$

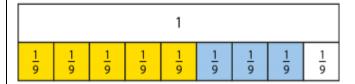
$$\frac{1}{8} + \frac{3}{8} + \frac{1}{8} = \boxed{}$$

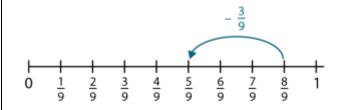
$$\frac{3}{16} + \frac{1}{16} = \frac{1}{16} + \frac{1}{16} + \frac{1}{16} + \frac{1}{16} + \frac{1}{16} + \frac{1}{16} + \frac{1}{16}$$



$$\frac{8}{9} - \frac{3}{9} = \frac{5}{9}$$







$$\frac{8}{9} - \frac{3}{9} = \frac{5}{9}$$

$$\frac{8}{10} - \frac{2}{10} = \frac{6}{10}$$

$$\frac{4}{17} + \frac{9}{17} - \frac{6}{17} = \boxed{}$$

Remind children that we say that addition and subtraction are the *inverse* of each other. This applies to addition and subtraction of fractions in the same way it applies to whole number calculations.

$$3 + 4 = 7$$

$$7 - 4 = 3$$

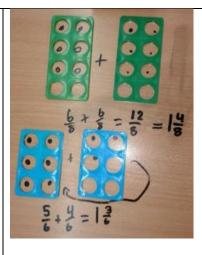
$$\frac{3}{10} + \frac{4}{10} = \frac{7}{10}$$

$$\frac{7}{10} - \frac{4}{10} = \frac{3}{10}$$

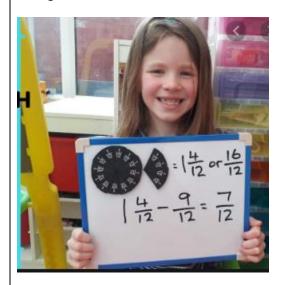
Year 4: National Curriculum: Fractions Recognise and show, using diagrams, families of common equivalent fractions. Count up and down in hundredths: recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten, solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number, Add and subtract fractions with the same denominator.

Key vocabulary: mixed numbers, improper fractions numerator, denominator, unit fraction, non-unit fraction, compare and order, halves, thirds, quarters, fifths, sixths, sevenths, eighths,

ninths, tenths, elevenths, twelf			
Objective and Strategies	Concrete	Pictorial	Abstract
Y4	Using numicon and pegs		
Add and subtract fractions with the same denominator	3/4 + 2/4 = 5/4 = 1 1/4	Use the models to add the fractions: $\frac{2}{7} + \frac{2}{7} =$	$\frac{2}{8} + \frac{4}{8} + \frac{1}{8} = \frac{7}{8}$
		$\frac{3}{5} + \frac{4}{5} =$	0 0 0
		Use a fraction number line + 2/5	$\frac{4}{5} + \frac{2}{5} = \frac{6}{5}$ or $1\frac{1}{5}$
	T	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	



Using fraction circles



Use the bar models to subtract the fractions.

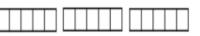


$$\frac{6}{7} - \frac{2}{7} =$$



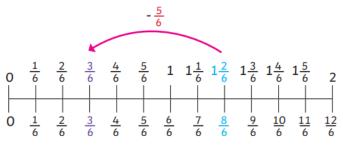


$$\frac{11}{6} - \frac{\Box}{6} = \frac{\Box}{6}$$



$$\frac{13}{5} - \frac{\square}{5} = \frac{6}{5}$$

Use a fraction number line



subtract fractions from a whole amount

$$2 - \frac{3}{4} =$$

$$\frac{8}{4} - \frac{3}{4} = \frac{5}{4}$$

	$2 - \frac{3}{4} =$	
Fractions of amounts	To find eighths of 56: 56	To find a fraction of a number, divide by the numerator and multiply by the numerator $ \frac{1}{8} 0 56 = 7 \frac{2}{8} 0 56 = 14 \frac{3}{8} 0 56 = 21 \frac{4}{8} 0 56 = 28 $ $ \frac{5}{8} 0 56 = 35 \frac{6}{8} 0 56 = 42 \frac{7}{8} 0 56 = 49 \frac{8}{8} 0 56 = 56 $

Year 5: National Curriculum: Fractions Compare and order fractions whose denominators are all multiples of the same number & identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths & recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, 5 2 + 5 4 = 5 6 = 1 5 1] & add and subtract fractions with the same denominator and denominators that are multiples of the same number & multiply proper fractions and mixed numbers by whole numbers, supported by materials and

Pictorial

Key vocabulary: Proper fractions, mixed numbers, improper fractions common numerator, common denominator, unit fraction, non-unit fraction, simplest form,

Y5

Add and subtract fractions with the same denominator and denominators that are multiples of the same number

Using a fraction wall/ tiles

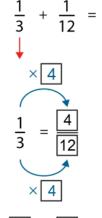
$$2/3 + 1/4 = 11/12$$

Concrete



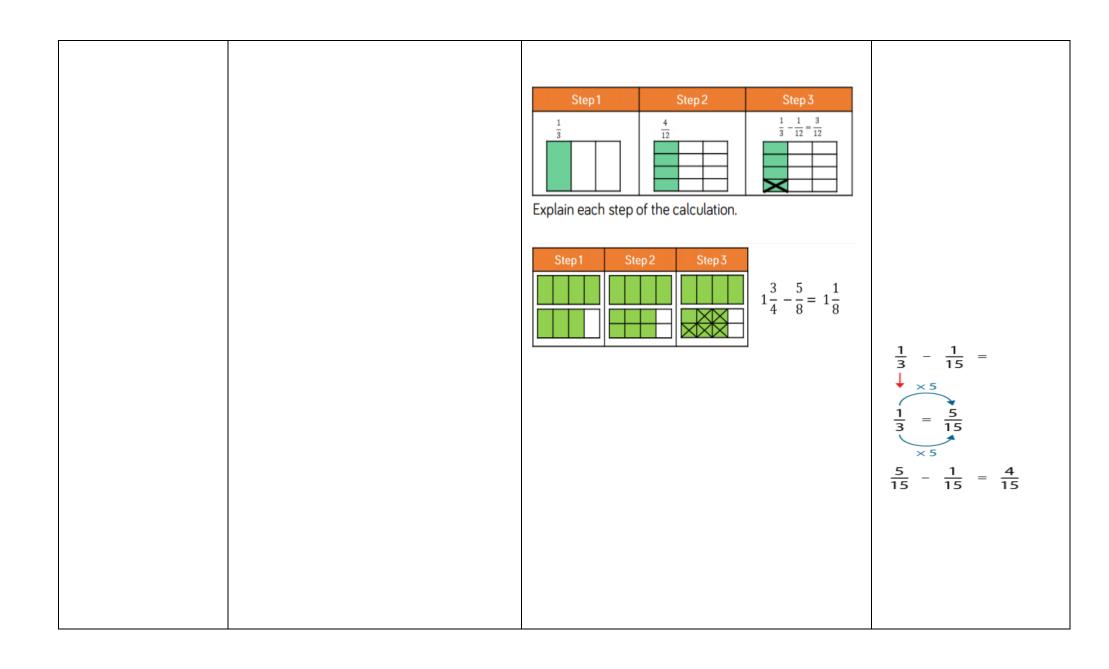
Step1	Step 2	Step 3
$\frac{1}{3}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
	1/6	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

$$\frac{1}{3} + \frac{1}{6} + \frac{1}{12} = 1$$
Explain each step of the calculation.
Use this method to help you add the fractions.



Abstract

$$\frac{4}{12} + \frac{1}{12} = \frac{5}{12}$$



Y5

Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams Using fraction circles

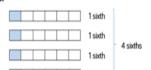


$$4 \times \frac{7}{8} \xrightarrow{\frac{7}{8}} \frac{7}{8}$$

Work out $\frac{1}{6} \times 4$ by counting in sixths.

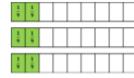
$$\frac{1}{6} \times 4 = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{4}{6} = \frac{2}{3}$$



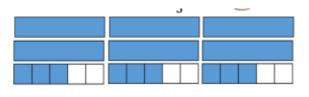


$$\frac{1}{6} \times 4 = \frac{4}{6} = \frac{2}{3}$$

Count the number of ninths to work $3 \times \frac{2}{9}$



$$2\frac{3}{5} \times 3$$



calculate $2\frac{3}{5} \times 3$

$$2 \times 3 = 6$$

$$\frac{3}{5} \times 3 = \frac{9}{5} = 1\frac{4}{5}$$

$$6 + 1\frac{4}{5} = 7\frac{4}{5}$$

Year 6: National Curriculum: Fractions * use common factors to simplify fractions; use common multiples to express fractions in the same denomination * compare and order fractions, including fractions > 1 * add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions * multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, 4 1 × 2 1 = 8 1] * divide proper fractions by whole numbers [for example, 3 1 ÷ 2 = 6 1

Key vocabulary: Proper fractions, mixed numbers, improper fractions common numerator, common denominator, unit fraction, non-unit fraction, simplest form, lowest terms, reduced, lowest common denominator

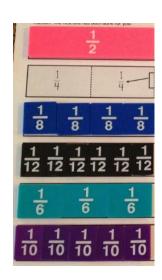
Objective and Strategies	Concrete	Pictorial	Abstract
Y6 How to teach: Add and subtract fractions with different denominators and mixed numbers			$\frac{5}{8} + \frac{3}{16}$ LCM of 8 and 16 is 16
mixed numbers			$\frac{5}{8} = \frac{10}{16}$
			$\frac{10}{16} + \frac{3}{16} = \frac{13}{16}$

Y6 Multiply simple pairs of proper fractions	$\frac{1}{5} \times \frac{1}{3} = \frac{1}{15}$ Is the same as $\frac{1}{5}$ of $\frac{1}{3}$	You may now choose to introduce the following generalisation: 'To multiply fractions, we can multiply the numerators and multiply the denominators.'
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\frac{1}{5} \times \frac{1}{3} = \frac{1}{15}$

Y6

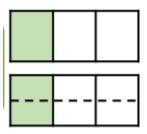
Divide proper fractions by whole numbers

Use a fraction wall



$$\frac{1}{4} \div 2 = \frac{1}{8}$$

 $\frac{1}{3} \div 2 = \frac{1}{6}$



1											
$\frac{1}{3}$ $\frac{1}{3}$					1/3						
1 12	1 12	1 12	1 12	1 12	1 12	1 12	1 12	1 12	1 12	1 12	1 12

To divide a fraction by a whole number, we can change it to an equivalent multiplication. To divide by 5 we can multiply by 1/5

$$\frac{1}{3} \div 5 = \frac{1}{15} \longrightarrow \frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$$

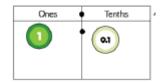
$$\frac{1}{3} \div 4 = \frac{1}{12} \checkmark$$

$$\frac{1}{3} \times \frac{1}{4} = \frac{1}{12} \checkmark$$

Year 4: National Curriculum: Decimals Recognise and write decimal equivalents of any number of tenths or hundredths. Recognise and write decimal equivalents to 1/4 1/2 3/4. Round decimals with one decimal place to the nearest whole number. Compare numbers with the same number of decimal places up to two decimal places. Find the effect of dividing a one or two digit number by 10 or 100. Identifying the value of the digits in the answer as ones, tenths and hundredths. Solve simple measure and money problems involving fractions and decimals to two decimal places

Key vocabulary: place value, rounding, decimal point, part-whole model, decimal equivalences, decimal tenths, tenths,.

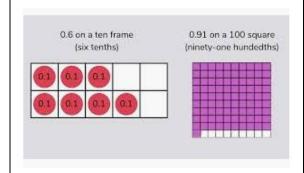
Objective and Strategies	Concrete	Pictorial					,	Abstrac	ot .				
Recognise and write decimal equivalents of any number of tenths and hundredths	te decimal uivalents of any mber of tenths			We can partition 56 hundredths into tenths and hundredths. Partition: 65 hundredths 31 hundredths 82 hundredths						Fraction	Decimal notation 0.1 0.01	Name one-tenth one- hundredth	
	Ones Tenths Ones Tenths Ones Tenths Ones Tenths Tenths There are ones and tenths. The decimal represented is	1,000 100 10 1 0.1 0.01	2,000 200 20 2 0.2 0.02	3,000 300 30 3 0.3 0.03	4,000 400 40 4 0.4 0.04	500 50 5 0.5	6,000 600 60 6 0.6 0.06	7,000 700 70 7 0.7 0.07	8,000 800 80 80 8 0.8	9,000 900 90 90 0.9 0.09			

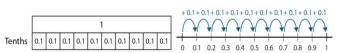


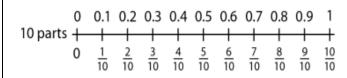
Write the decimal represented in each place value grid.

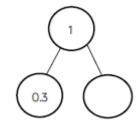
Ones	Tenths	Hundredths	The decimal represented i
			There are hundredths.
•	•	• •	
Ones	Tenths	Hundredths	There are tenths.

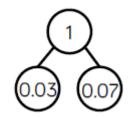
Tens frame and place value counters

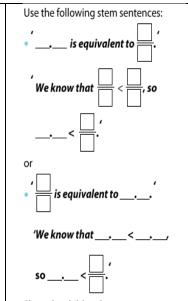


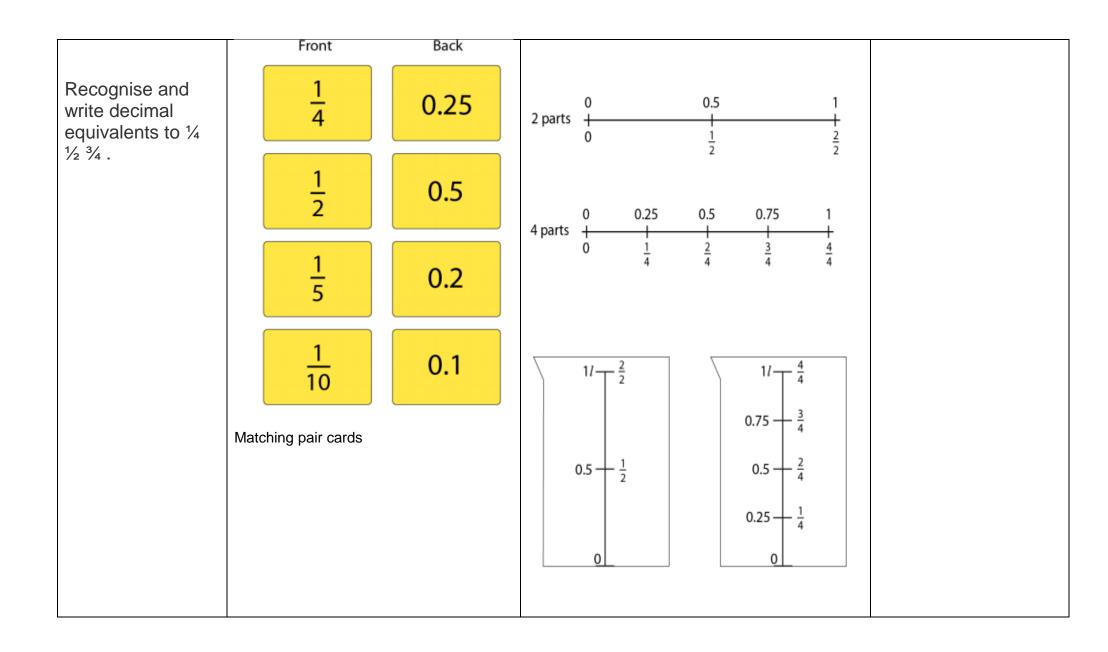


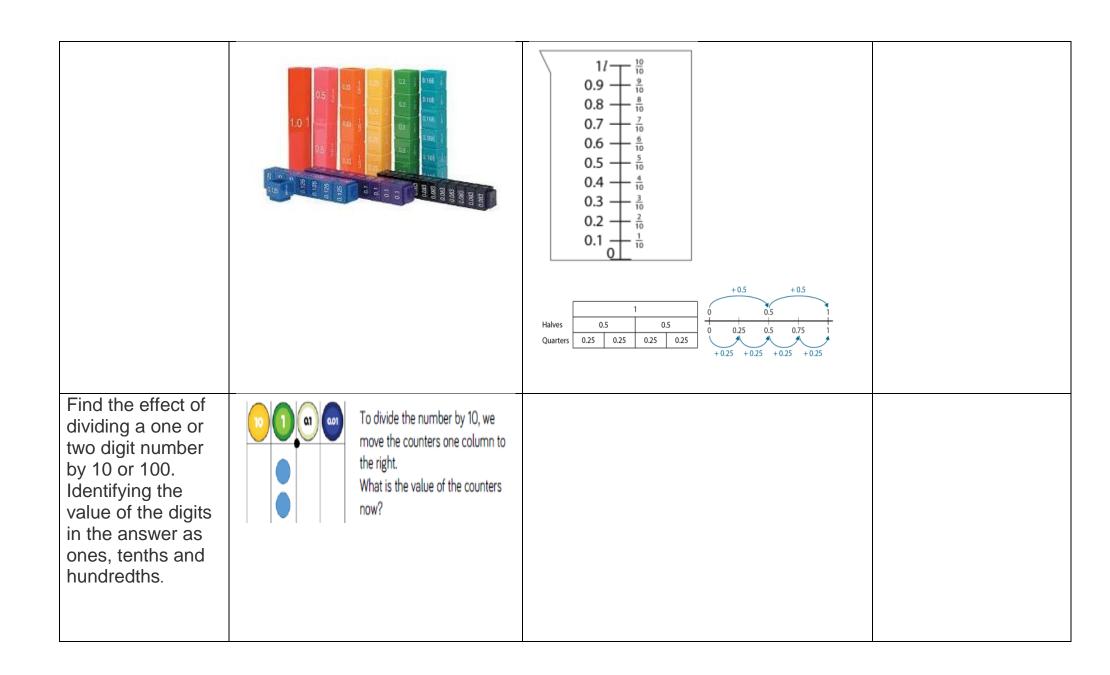








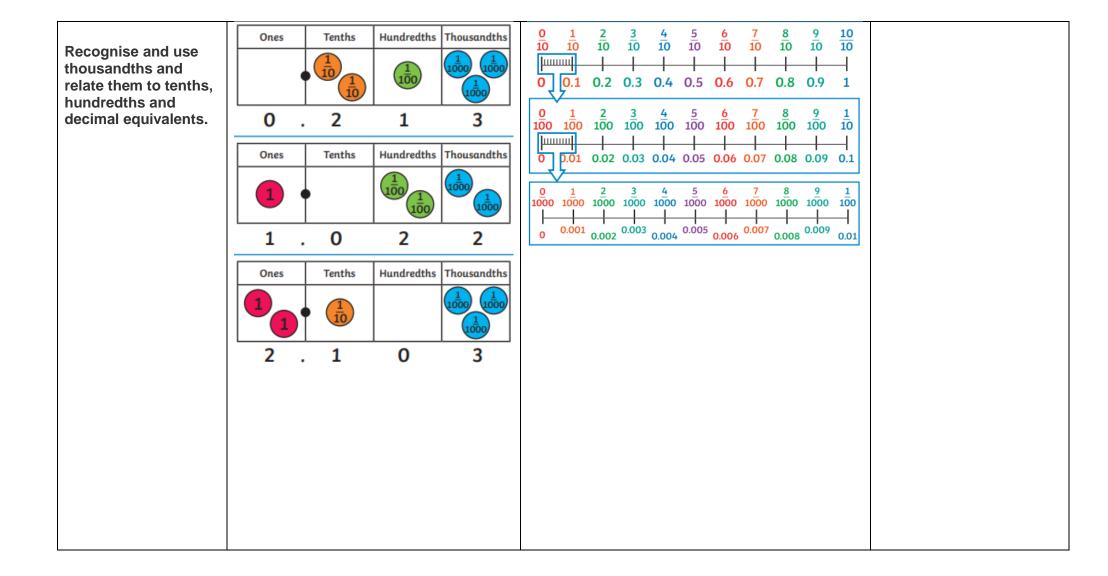


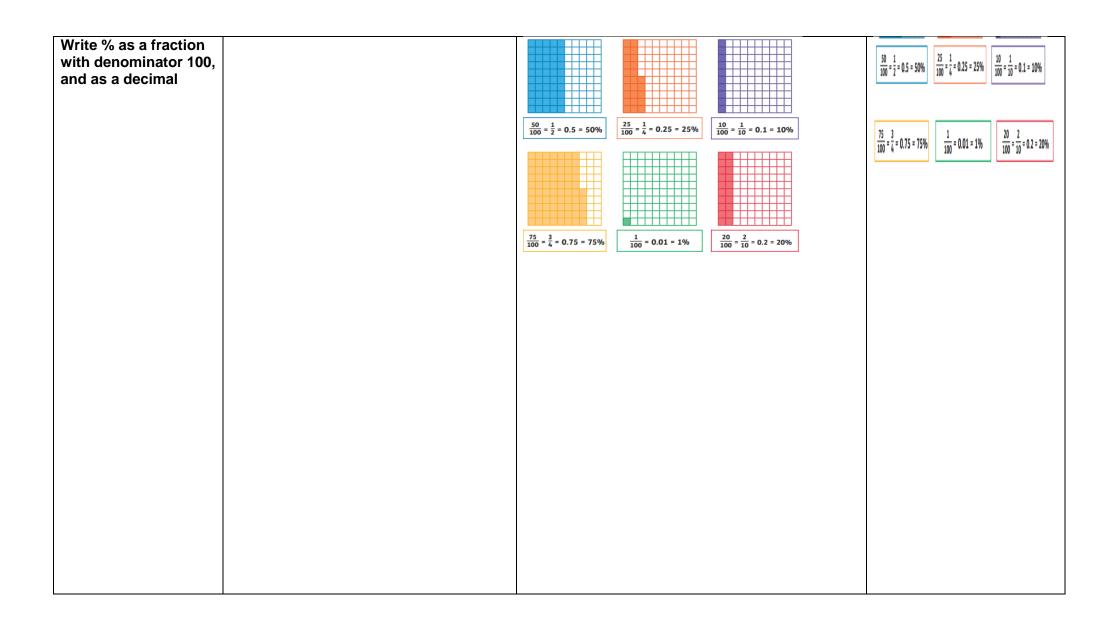




Key vocabulary: place value, rounding, decimal point, part-whole model, decimal equivalences, decimal tenths, decimal hundredths, tenths, hundredths.

Objective and Strategies	Concrete	Pictorial	Abstract
Read and write decimal numbers as fractions	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$0.71 = \frac{71}{100} = \frac{7}{10} + \frac{1}{100}$ $0.37 = \frac{37}{100} = \frac{3}{10} + \frac{7}{100}$





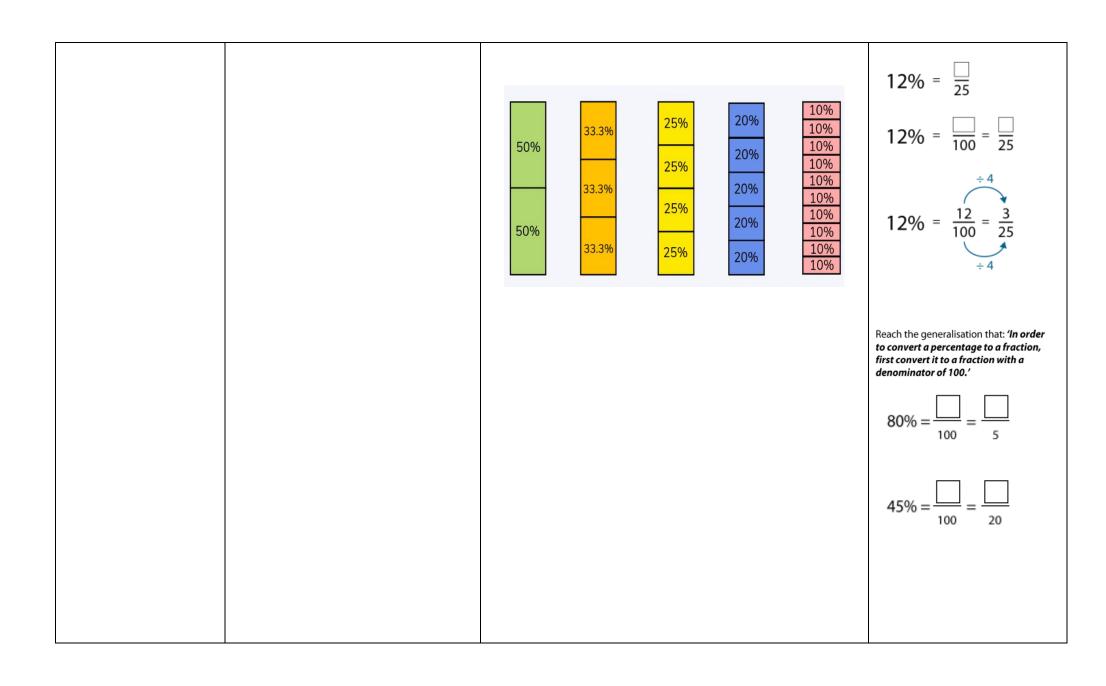
Year 6: National Curriculum: Decimals & Percentages] * associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 8 3] * identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places, multiply one-digit numbers with up to two decimal places by whole numbers * use written division methods in cases where the answer has up to two decimal places * solve problems which require answers to be rounded to specified degrees of accuracy * recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.

Key vocabulary: decimal place, decimal fraction, recurring decimal, equivalent fraction, tenth, sharing, partitioning, exchanging, rounding to 3d.p,

hundredth, thousandth, equal to, remainder, grouping

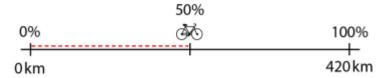
	, equal to, remainder, grouping							
Objective and Strategies	Concrete	Pictorial	Abstract					
Identify the value of each digit in numbers given to three decimal places.	Ones							
	There are ones, tenths, hundredths and thousandths. The number in digits is							

Objective and Strategies	Concrete	Pictorial	Abstract
Associate a fraction with division and calculate decimal fraction equivalents. Recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.		Percentage Fraction Hundred square Number line	FractionDecimal $\frac{1}{2}$ 0.5 $\frac{1}{3}$ 0.333333 $\frac{1}{4}$ 0.25 $\frac{1}{5}$ 0.1666 $\frac{1}{7}$ 0.14285714 $\frac{1}{9}$ 0.111 $\frac{1}{10}$ 0.1Highlight $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$ and $\frac{1}{10}$ (two parts, four parts, five parts and ten parts, respectively). These are most common divisions used in graphs and measures. As such, they will be the focus of our learning. Because these fraction-decimal equivalents are so important and frequently used, it is necessary to learn them off by heart. $\frac{1}{8}$ is not as commonly used as the other fractions, but it is a fraction that can also be useful to know the decimal equivalent of.



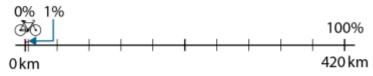
Find percentages of amounts

'Zara is doing a 420 km charity bike ride. So far, she has completed 50% of the route. How far has she cycled?'



- '100% of 420 km is 420 km.'
- '50% of 420 km is ¹/₂ of 420 km.'
- 'Zara has cycled 210 km.'

'James has completed 1% of the same bike ride. How far has he cycled?'

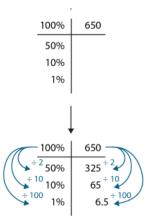


- '100% of 420 km is 420 km.'
- '1% of 420 km is $\frac{1}{100}$ of 420 km.'
- 'James has cycled 4.2 km.'

Work towards the following generalisation: 'To find 50% of a number, halve it.'

Work towards the following generalisation: 'To find 10% of a number, divide it by ten.'

Work towards the following generalisation: 'To find 1% of a number, divide it by one hundred.'



	I	
		,
	1009	6 420km
	509	6 210km
	259	6 105km
	759	6 315km
	Finding 75% of 420:	
	Method 1	
	75% of 420 = 210 + 105	
	= 315	
	Method 2	
	$75\% \text{ of } 420 = 105 \times 3$	
	= 315	
	Method 3	
	75% of 420 = 420 – 105 = 315	
	Find 45% of 64.	,
	100% 64	
	50% 32	
	10% 6.	_
	5% 3	
	Method 1:	
	45% of 64=3	32-3.2
	= 2	28.8
	Method 2:	
	45% of 64=4	1 × 6.4 + 3.2
		25.6 + 3.2
	= 2	28.8

Calculate the whole amount from the part %	Bar model: 60% 300 100 100 100 20% 20% 20% 60% 300 100 100 100 100 100 20% 20% 20% 20% 20%	
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